



professionals or researchers.

Mathematics is a universal language. Differential equations, mathematical modeling, numerical methods and computation form the underlying infrastructure of engineering and the sciences. In this context mathematical modeling is a very powerful tool for studying engineering problems, natural systems and human society. This interdisciplinary book contains comprehensive modeling of casting processes requires the development of flexible numerical tools which can handle multiple phenomena (e.g., mold filling, heat transfer, solidification phase change, shrinkage, segregation, etc.) occurring in arbitrary geometries. In this thesis, a range of robust and efficient numerical algorithms for the analysis of casting processes is developed. The focus is on methods which can handle coupled filling and solidification. In the first place, modeling of solidification processes and associated phenomena is considered. A consistent set of transport equations governing the solidification of a metallic alloy is presented. On considering increasingly sophisticated versions of these transport equations, a general fixed grid numerical algorithm is developed. Following this, the usefulness of the algorithm is demonstrated on application to a range of solidification examples taken from recent literature. These include heat conduction driven problems, problems with convection, as well as problems with shrinkage and segregation. Next, numerical modeling of the mold filling process is considered. A consistent set of transport equations governing the filling of molten metal into a mold shape is presented. A brief review of existing methods used to track the free surface between the metal and air is provided. The limitations of existing fixed grid methods, in particular, the requirement for an explicit time integration, the need for special procedures to ensure a sharp interface and the inability to handle arbitrary geometries are discussed. A new fixed grid algorithm which overcomes these limitations is derived. The utility of this algorithm is demonstrated on application to a range of example problems. Finally, the two algorithms are coupled and an analysis tool for concurrent filling, heat transfer and phase change is developed. This tool is used to simulate sand and permanent mold casting processes as well as reaction injection molding of polymers. Throughout the thesis, the efficiency of the proposed algorithms is demonstrated by making ample CPU comparisons with previous filling and solidification algorithms. The algorithms developed in this thesis are implemented on both finite difference and finite element grids. Heat and Mass Transfer in Drying of Porous Media offers a comprehensive review of heat and mass transfer phenomena and mechanisms in drying of porous materials. It covers pore-scale and macro-scale models, includes various drying technologies, and discusses the drying dynamics of fibrous porous material, colloidal porous media and size-distributed particle systems. Providing guidelines for mathematical modeling and design as well as optimization of drying of porous material, this reference offers useful information for researchers and students as well as engineers in drying technology, food processes, applied energy, mechanical, and chemical engineering.